

# Synergistic effect of radial electric field and magnetic shear on ion temperature gradient mode

Qien Jing<sup>1</sup>, Yuehao Ma<sup>2</sup>, Zhihong Lin<sup>3</sup>, Huishan Cai<sup>2,\*</sup>

<sup>1</sup>University of Science and Technology of China, Hefei 230026, China

<sup>2</sup>CAS Key Laboratory of Frontier in Controlled Nuclear Fusion, and School of Nuclear Sciences and Technology, University of Science and Technology of China

<sup>3</sup>Department of Physics and Astronomy, University of California, Irvine, CA 92697, United States of America

E-mail: [hscai@mail.ustc.edu.cn](mailto:hscai@mail.ustc.edu.cn)

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**Abstract.** Based on the Gyrokinetic Toroidal Code (GTC), the synergistic effect of the radial electric field ( $E_r$ ) shear and the magnetic shear on ion temperature gradient (ITG) instabilities of an Experimental Advanced Superconducting Tokamak (EAST) discharge (#93890) is studied. It is found that the synergistic effect of the magnetic shear and the  $E_r$  shear is significant in stabilizing ITG mode. Whether the  $E_r$  shear plays a stable role or destabilizing role depends on both the relative direction of the  $E_r$  shear and the magnetic shear, and the amplitude of the  $E_r$  shear. Specifically, the  $E_r$  shear with negative shearing rate has more efficient stabilizing effect under the weakly reverse magnetic shear. Based on the experimental  $E_r$  profile, it is shown that the global effect of  $E_r$  on the stabilization of micro-instabilities needs to be considered. The  $E_r$  with the  $\omega_s = 0$  at the inner side of the ITG mode shows a better stabilizing effect, because of the synergistic effect of negative shearing rate and weakly reverse magnetic shear at the ITG mode location. The results indicate that the positive feedback between the formation of ITB and the formation of  $E_r$  well with an optimized magnetic shear might be the key to the long-time existence of ITB.

Keywords: radial electric field, ion temperature gradient, magnetic shear, EAST plasma

## 1. Introduction

In a tokamak, ion temperature gradient (ITG) micro-instabilities dominate the ion heat transport channel, could be unfavorable to plasma confinement. Inside the internal transport barrier (ITB), the gradient of temperature or density is high, due to the reduction of anomalous transport caused by turbulence. Most theoretical models for ITB formation ultimately rely on the stabilization of micro-instability induced transport by the magnetic shear and the sheared  $E \times B$  flows [1, 2, 3]. Previous studies have shown that the  $E_r$  shear plays an important role in tokamak because it has a stabilizing effect on microturbulence and reduces the turbulent transport level to improve the plasma confinement [4, 5, 6, 7]. It has been experimentally confirmed on tokamak that increase in shear rate ( $\omega_{E \times B}$ ), which is normally used for describing the strength of the sheared flow, would stabilize ITG instabilities and promote the formation of ITB [8]. On the other hand, the appropriate magnetic shear can stabilize the instability and be in favor of the formation of ITB [1, 9]. Therefore, understanding the synergistic effect of the  $E_r$  shear and the magnetic shear on stabilizing ITG instabilities is significant for improving the operational stability of fusion plasma. Previous simulation studies showed that  $E_r$  shear always plays a stabilizing role on ITG under different magnetic shears [4, 5], despite the effect is enhanced with increasing magnetic shear [3].

The appropriate magnetic shear and the  $E_r$  shear will both tilt the structure of the ballooning mode and reduce the growth rate of the mode [2, 3, 4]. However, the different direction of these shear effect will tilt mode structure in different direction. Therefore, the synergistic effect of the  $E_r$  shear and the magnetic shear is important because the synergistic effect determines the tilting direction of the mode structure, which might cause the  $E_r$  shear become a destabilizing effect. Based on these physical considerations, in this work, the performance of the synergistic effect of the  $E_r$  shear and the magnetic shear on ITG instabilities on EAST are studied using the gyrokinetic toroidal code (GTC).

The remainder of this paper is organized as follows. The physical model and simulation setup are described in section 2. The stabilizing performance of synergistic effect of the  $E_r$  shear and magnetic shear on microturbulence is discussed in section 3. The further research using the experimental  $E_r$  profile is discussed in section 4. Section 5 gives a summary of the study.

## 2. Physical model and simulation setup

This study focuses on the synergistic effect of equilibrium radial electric fields and magnetic shear on electrostatic drift wave turbulence. The detail of the gyrokinetic models utilized in the GTC code have been previously discussed in [4, 10, 11]. To account for the influence of the equilibrium radial electric field  $E_r$ , the electrostatic potential  $\phi = \delta\phi + \phi_{eq}$  is incorporated into the gyrokinetic equations [4], where  $\phi_{eq}$  is the equilibrium electrostatic potential[2].

The equilibrium electric field will impact the ITG plasma in two important ways. Firstly, the rigid rotation caused by  $E \times B$  drift will change the frequency of the ITG mode, i.e. doppler shift  $\Omega_E = -nd\phi_{eq}/d\psi$  [12]. Secondly, the sheared flow caused by  $E_r$  will reduce the linear growth rate of ITG mode and affect the saturation amplitude.

In our study, the simulations of electrostatic turbulence are conducted using experimental data from EAST tokamak discharge (#93890) at 5000ms, where both the plasma profile and magnetic geometry have previously been discussed in [11, 13]. As shown in Fig. 1, both the electron and ion densities, as well as temperatures, exhibit an internal transport barrier (ITB) in the presence of weakly negative magnetic shear. Our simulation domain is delineated in the radial normalized range  $r/a \in [0.10, 0.52]$ , as indicated by the gray dashed line in Fig. 1. Dirichlet boundary conditions are applied due to the negligible turbulence perturbations near the boundary. The other simulation parameters used for convergent physical run are 150 radial grids, 32 toroidal grids and 600 poloidal grids in the simulation domain. The time step is  $\Delta t = 0.005R_0/C_s$  (where  $C_s$  is the sound speed on magnetic axis).

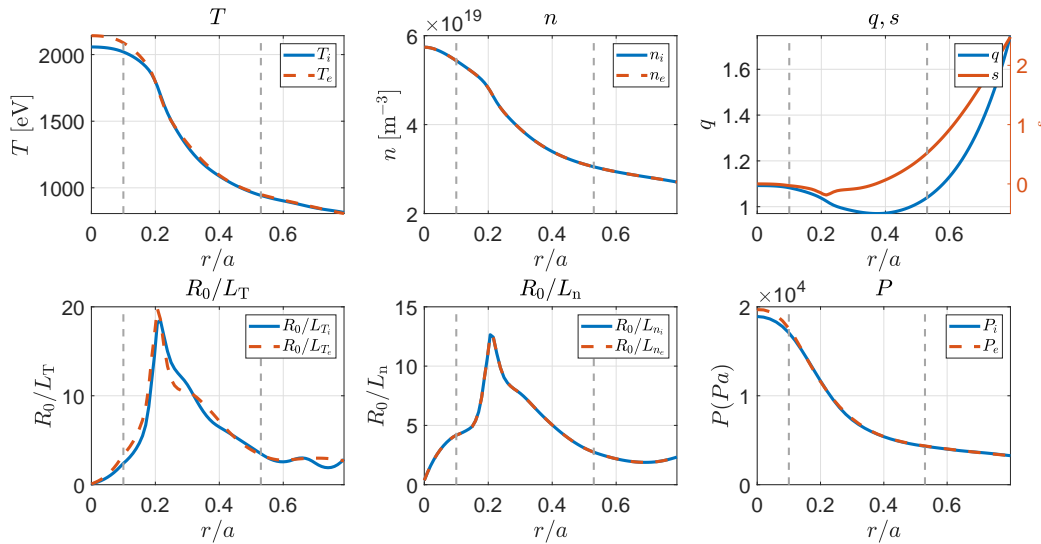


Figure 1: Plasma radial profile in EAST discharge #93890 at 5000 ms, and the simulation region is noticed by gray dashed line. The top row, from left to right, shows temperatures ( $T$ ), density ( $n$ ) for ions (subscript  $i$ ) and electrons (subscript  $e$ ), safety factor ( $q$ ) and magnetic shear ( $s$ ) respectively. The bottom row, from left to right, shows the inverse temperature length scales ( $R_0/L_T$ ), the inverse density length scale ( $R_0/L_n$ ), pressure for ions and electrons respectively.

### 3. Radial electric field shear effects on ITG

#### 3.1. ITG mode dispersion relation and frequency Doppler shift caused by $E_r$ shear

To study the performance of the synergistic effect of the  $E_r$  shear and the magnetic shear on stabilizing ITG instabilities, the dispersion relation with  $E_r$  should be verified in the physical model. The dispersion relation without  $E_r$  in the simulation domain has

been well researched previously in the report [11], showing that the peak value of the ITG linear growth rate  $\gamma$  is  $k_\theta \rho_i \approx 1$  ( $n = 25$ ). Now, we use a constant  $d\phi/d\psi$  ( $\omega_s = 0$ ) profile to verify the Doppler shift effect on ITG mode, where  $\omega_s = -\frac{(R_0 B_p)^2}{B_0} \partial^2 \phi_{eq} / \partial \psi^2$  is shearing rate [4]. The simulation results of the mode frequency, both without  $E_r$  and with  $E_r$  ( $\omega_s = 0$ ), are depicted in Fig. 2a.

The simulation results with  $E_r$  ( $\omega_s = 0$ ) agree well with the theoretical results calculated by the Doppler shifted effect [12]. Additionally, the linear growth rates without  $E_r$  and with  $E_r$  ( $\omega_s = 0$ ) have no obvious difference, indicating the  $E_r$  with  $\omega_s = 0$  has nearly no stabilizing effect on ITG mode. The Doppler shift effect of the ITG mode is similar to the results on CBC case [4].

Moreover, to verify the impact of the  $E_r$  shear on the linear growth rate of modes, we scan different toroidal numbers  $n$  under  $E_r$  with constant  $\omega_s = 0, 0.1$ , which is shown in Fig. 2b. The  $n = 25$  mode is the most unstable mode under different constant  $\omega_s$ . However, the presence of  $E_r$  shear increases the growth rate, which is different from the result where  $E_r$  shear decreases the growth rate of ITG mode [4, 5, 6]. Next, we focus on the most unstable case ( $n = 25$ ) to study the effect of  $E_r$  shear on ITG mode.

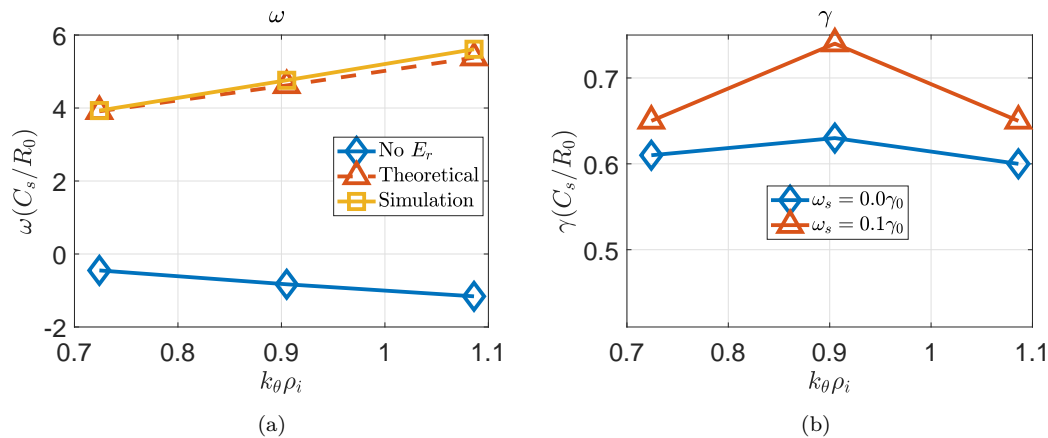


Figure 2: (a) shows the mode frequency of ITG mode are represented by the blue line (without  $E_r$ ), the orange line (with  $\omega_s$  for  $E_r$ ) and the red dashed line (theoretical results), respectively. (b) shows the linear growth rate of ITG versus poloidal wavenumber  $k_\theta \rho_i$  (corresponding to toroidal mode number  $n = 20, 25, 30$ ) under constant  $\omega_s/\gamma_0 = 0.0, 0.1$ , where  $\gamma_0$  is the growth rate without  $E_r$ . The  $E_r$  profile with constant  $\omega_s$  are shown in Fig. 3a.

### 3.2. Stabilizing effects on ITG mode of the $E_r$ shear

In the cases followed, the constant shearing rate  $\omega_s$  is scanned. The ITG growth rate versus  $\omega_s$  in simulation are shown in Fig. 3. For  $\omega_s > 0$ , the growth rate initially increases with  $\omega_s$ . As  $\omega_s$  becomes large enough, the growth rate then decreases with  $\omega_s$  increasing. The peak value of the linear growth rate corresponds to  $\omega_s/\gamma_0 = 0.1$ . For  $\omega_s < 0$ , the growth rate monotonically decreases with increasing  $|\omega_s|$ . Specially, the effect of negative shearing rate is more effective in comparison with the effect of positive

shearing rate on ITG. These results shows that the stabilizing effect of the  $E_r$  shear depends on the sign of the shear, which is different from the result shown in previous researches [4, 5, 6]. The Fig. 4 shows mode structures of  $\delta\phi$  correspond to the results shown in Fig. 3. As shown in Fig. 4c, without  $E_r$  shear ( $\omega_s = 0$ ), the ballooning angle  $\theta_0$  [14, 15, 16] is greater than zero. With the increase of positive  $\omega_s$ , the  $E_r$  tilts the ITG mode structure clockwise so that the  $\theta_0$  initially decreases to zero, which is shown in Fig. 4d, and then monotonically decreases, which is shown in Fig. 4e, 4f. With the increase of negative  $\omega_s$ , the  $E_r$  tilts the ITG mode structure anticlockwise so that the  $\theta_0$  monotonically increases.

The decrease in the ITG growth rate due to the  $E_r$  shear is associated with the tilt of the ITG mode structure. The mode structure tilts itself can reduce ITG mode growth rate [5]. On the other hand, the tilt increase  $|\theta_0|$ , which will increase the effective  $k_r$  and reduce the linear growth rate [6, 2]. Combining this mechanism, the above results of  $E_r$  shear on ITG can be understood. In the above cases on EAST, the weakly reverse magnetic shear near the ITG location,  $s = -0.13$ , tilts the flute-like mode structure [3] as shown in Fig. 4c. From Fig. 4d, the  $E_r$  with positive  $\omega_s$  partly cancels the tilting effect of the weakly reverse magnetic shear, causing the ITG mode growth rate initially increases with the increasing positive  $\omega_s$ . When the positive  $\omega_s$  is large enough, the tilting effect caused by  $E_r$  shear is dominant compared with magnetic shear as shown in Fig. 4e–4f. Consequently, the ITG mode growth rate decreases with the increasing positive  $\omega_s$ . For the  $E_r$  with negative  $\omega_s$ , the tilting direction of the  $E_r$  shear and the magnetic shear are same, the ITG mode growth rate monotonically decreases with increasing magnitude of negative  $\omega_s$ . Therefore, the stabilize effect of the sheared flow caused by the  $E_r$  shear on EAST depends on the sign of shearing rates  $\omega_s$  and the negative  $\omega_s$  shear is more effective than positive  $\omega_s$  shear in stabilizing the ITG mode on EAST. This is different from the CBC case, where the ballooning angle  $\theta_0 \rightarrow 0$  for ITG with the magnetic shear  $s \approx 0.8$  at the location of maximum ITG mode amplitude in the radial direction in the absence of electric field [4, 5]. Thus, the effects of  $E_r$  shear on ITG in the CBC case are all stabilizing. Hence, the synergistic effect of  $E_r$  and magnetic shear on ITG is important. Whether the  $E_r$  shear plays a stabilizing role or not depends on the net effect contributed from the magnetic shear and the  $E_r$  shear.

### 3.3. Synergistic effect of $E_r$ shear and magnetic shear on EAST

The synergistic effect of the  $E_r$  shear and the magnetic shear on EAST is further investigated in this section. We use different  $q$  profiles to obtain different magnetic shear ( $s = -0.13, 0.2, 0.4, 0.6, 0.8$  at the ITG location without  $E_r$  shear) and compare the stabilizing effects on ITG mode of the  $E_r$  shear under different magnetic shear.

The  $q$  profiles we used are shown in the Fig. 5a. The Fig. 6a shows that, without  $E_r$ , the ITG growth rate  $\gamma$  increases with the increasing magnetic shear within  $s \in [-0.13, 0.8]$ . Because the decreasing magnetic shear tilts the ITG mode streamer more strongly and decreases the ITG growth rate, which is shown in Fig. 7a–7c. This

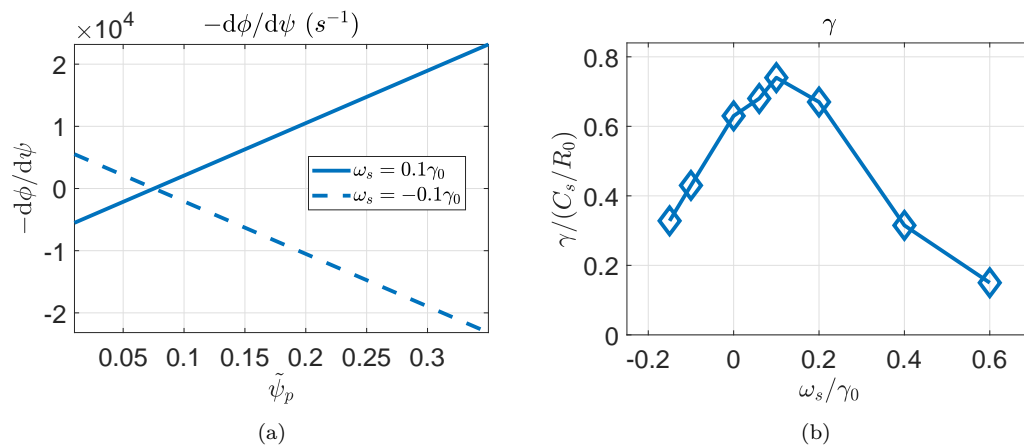


Figure 3: (a) The  $E_r$  with  $\omega_s/\gamma_0 = \pm 0.1$  represented by  $d\phi/d\psi$  over normalized poloidal flux and the  $E_r$  with  $\omega_s/\gamma_0 = -0.15, 0.20, 0.40, 0.60$  is generated by changing the slope of the  $d\phi/d\psi$ . Noticed that the  $\omega_s = 0$  is set at the location of ITG, therefore, the doppler shift effect is not necessary to be considered. (b) Simulations results of the growth rate versus shearing rate  $\omega_s$  with constant  $\omega_s$ .

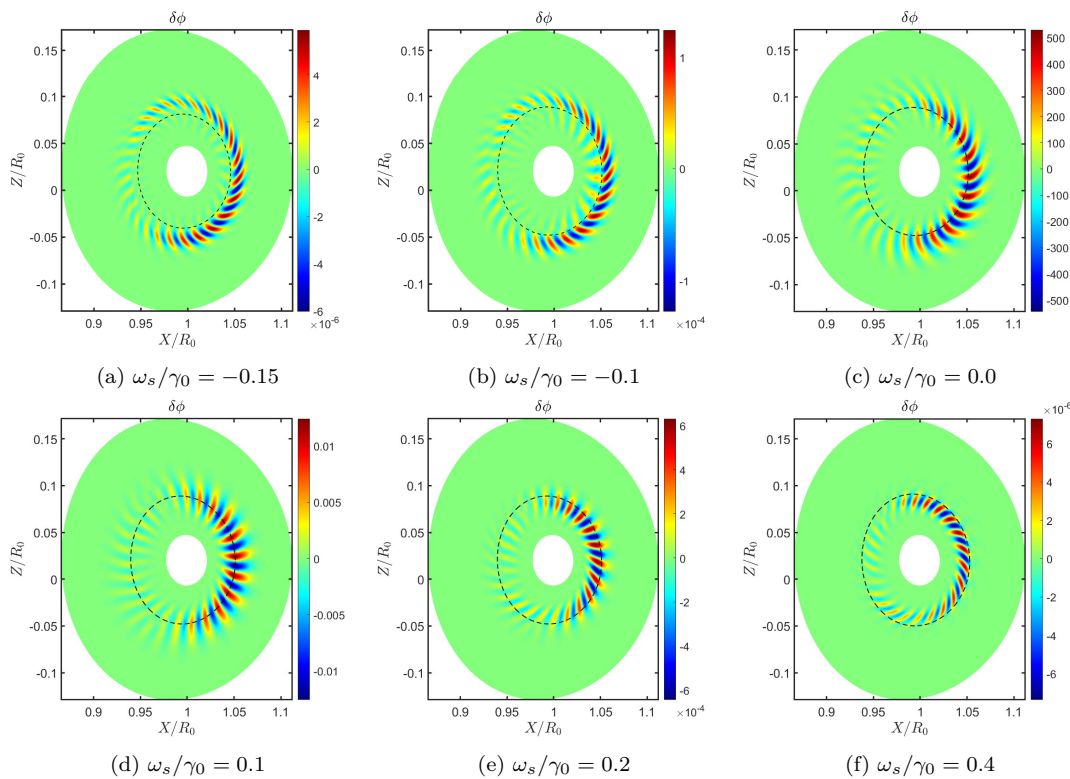


Figure 4: The poloidal mode structure of the real part of electrostatic potential with constant  $\omega_s/\gamma_0 = -0.15, -0.1, 0.0, 0.1, 0.2, 0.4$ . The dashed line indicates the largest  $\eta_i$  and  $q = 1$  positions. Noted that these six mode structures are extracted from the same physical time point in same simulation conditions, the magnitudes in each figure can be directly compared.

explanation follows the mechanism we discussed in the above section. Additionally,  $E_r$  shear twists the eddy of ITG mode to good curvature direction that reduces the linear growth rate [3], which are shown in Fig. 7a–7c. Besides, the different  $m$  harmonic

coupling also contributes to the linear growth rate decrease, which is shown in Fig. 7d–7f.

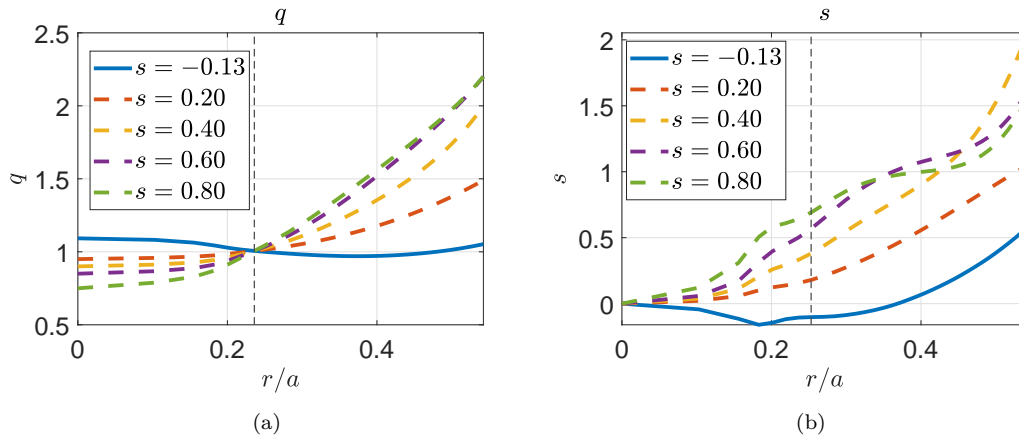


Figure 5: (a) The  $q$  profiles we used to create different  $s$ . (b) Profiles of magnetic shear ( $s$ ). Noticed that the value of  $s$  in legend corresponds the value at the ITG location which is indicated with gray dashed line.

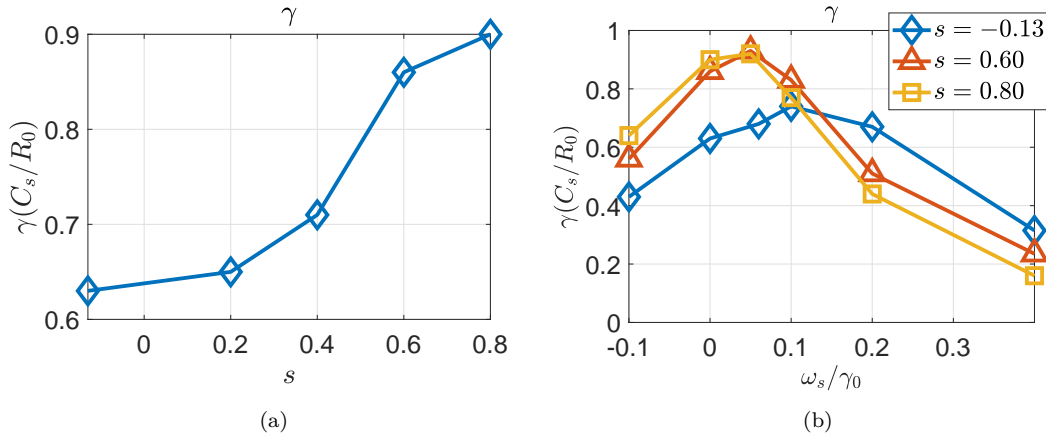


Figure 6: (a) ITG growth rate  $\gamma$  over magnetic shear  $s$  without  $E_r$ . (b) The ITG growth rate  $\gamma$  versus  $\omega_s$  with  $s = -0.13, 0.6, 0.8$  shown in Fig. 5b, respectively.

With the understanding of magnetic shear tilting effect on ITG mode, the synergistic effect of  $E_r$  shear and magnetic shear is investigated. We scan the ITG linear growth rate  $\gamma$  versus  $\omega_s$  under different magnetic shear, which is shown in Fig. 6b. Under the higher magnetic shear ( $s = 0.6, 0.8$ ), the shearing rate corresponds to the maximum linear growth rate is  $\omega_s/\gamma_0 \approx 0.05$ , which is smaller than the one ( $\omega_s/\gamma_0 \approx 0.10$ ) that under the weakly reverse magnetic shear ( $s = -0.13$ ). Moreover, the  $E_r$  with negative  $\omega_s$  is more effective in stabilizing ITG under the weakly reverse magnetic shear ( $s = -0.13$ ) compared to the higher magnetic shear. That is because the tilting effect caused by the higher magnetic shear ( $s = 0.6, 0.8$ ) is weak and the ballooning is  $\theta_0 \approx 0$ , which is shown in Fig. 7c. As a result, the  $E_r$  shear become dominant in tilting the ITG mode. From Fig. 6b, the peak value of linear growth rate with normal positive magnetic



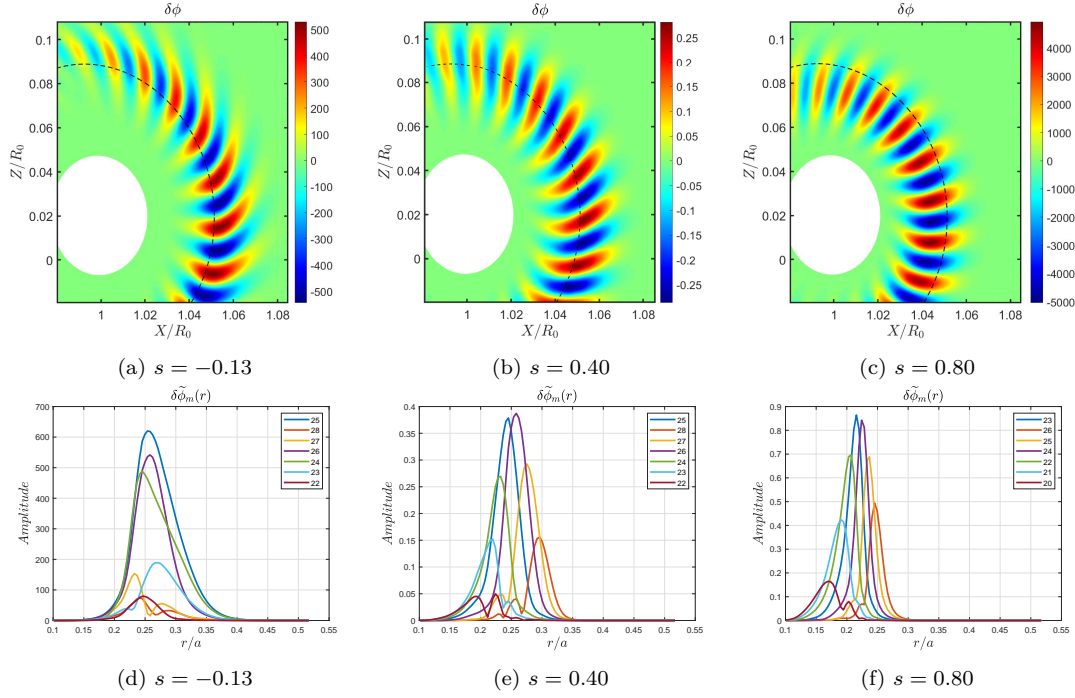


Figure 7: (a)-(c) show the poloidal mode structure of the real part of electrostatic potential with magnetic shear  $s = -0.13, 0.40, 0.80$  shown in Fig. 5b, respectively. (d)-(f) show the radial mode profile of different poloidal mode numbers  $m$  corresponding the mode structures in top panels.

shear ( $s = 0.6, 0.8$ ) is obviously higher than case with weakly negative magnetic shear ( $s = -0.13$ ). These indicate that it is important to optimize the magnetic shear and the  $E_r$  shear simultaneously in order to maximize the stabilizing effect of the  $E_r$  shear.

#### 4. Simulation with experimental $E_r$ on EAST

We use the parameters based on a ITB formed case at  $5000ms$  on EAST [13] to calculated experimental  $E_r$  profile from the radial force balance equation:

$$\partial\phi_{eq}/\partial\psi = -\frac{1}{n_i Z_i} \partial P_i / \partial\psi + q\Omega_\theta - \Omega_\phi \quad (1)$$

where  $n_i$  and  $P_i$  are the ion density and pressure,  $q$  is the safety factor,  $\Omega_\theta$  is the poloidal rotation,  $\psi$  is the poloidal flux. However, we focus on the experiments with a weak torque so that the ion pressure gradient is the dominant term in the radial force balance equation and the effects of rotation terms can be ignored [13]. Based on the radial electric field of the experimental configuration as shown in Fig. 8a, we carry out the linear simulation test and find that the ITG mode can be fully stabilized. To better understand the performance of ITG mode under the experimental  $E_r$  profile, we consider the amplitude of the  $E_r$  and the  $\omega_s = 0$  location of the  $E_r$ . Because the ITG mode structure has a small radial scale, there may be no shearing effect on ITG at the position where  $\omega_s = 0$ .

Firstly, by multiplying the  $E_r$  profile by a coefficient, we change the amplitude of



the  $E_r$  profile. The simulation results are shown in Fig. 8b, where the maximum value of the shearing rate  $\omega_s^{max}$  is used to measure the amplitude of the  $E_r$  profile.

The linear growth rate decreases more obviously under the experimental  $E_r$  profile, indicating that the  $E_r$  well is more efficient than the  $E_r$  with constant  $\omega_s$  on stabilizing the ITG mode.

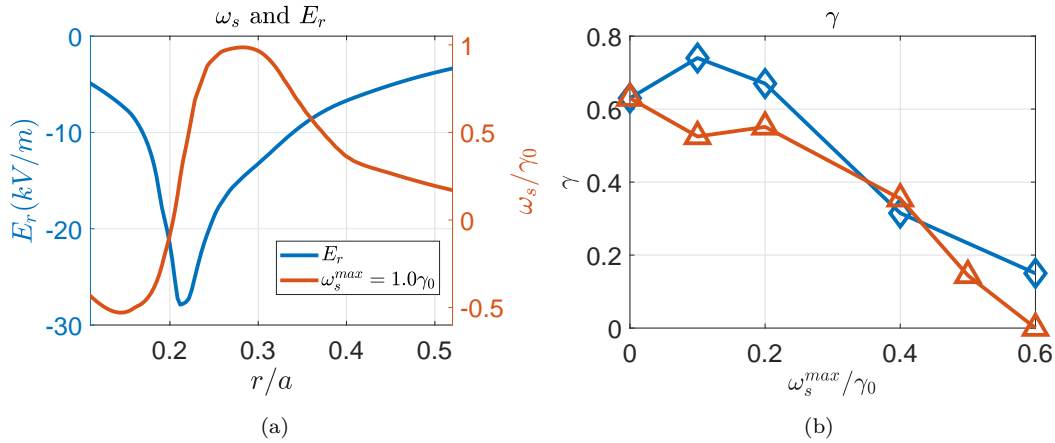


Figure 8: (a) Left y axis is the experimental  $E_r$  directly calculated by the radial force balance equation and the right y is the corresponding shearing rate. (b) The blue line represents the ITG growth rate versus  $\omega_s^{max}$  for  $E_r$  profile with different constant  $\omega_s$ . The red line denotes the ITG growth rate versus  $\omega_s^{max}$  for different amplitude of experimental  $E_r$  profile with  $\omega_s = 0$  at  $r/a = 0.20$  as shown in Fig. 8a.

Secondly, the different locations of  $\omega_s = 0$  are studied. The  $\omega_s = 0$  location at  $r/a = 0.20, 0.25, 0.30$  are studied, where  $r/a = 0.25$  is the location of ITG.  $r/a = 0.20$  and  $r/a = 0.30$  denote the  $\omega_s = 0$  surface located at the left hand and right hand of the ITG mode, respectively. The  $E_r$  profile with different  $\omega_s = 0$  location is created by shifted original  $E_r$  profile in radial space. We scan  $\omega_s^{max}/\gamma_0 = 0.2, 0.4, 0.6$  for each  $\omega_s = 0$  setting. The simulation results are shown in Fig. 9a. In comparison with the results with  $\omega_s = 0$  location at  $r/a = 0.20$  (at the left hand side of the mode), when  $\omega_s = 0$  location at  $r/a = 0.30$  (at the right hand side of the mode), for  $\omega_s^{max}/\gamma_0 = 0.2, 0.4, 0.6$ , the ITG mode at the  $q = 1$  is fully stabilized, showing that the  $E_r$  stabilizing effect is more effective because of the  $E_r$  with negative  $\omega_s$  at the ITG mode location. This result matches the physical mechanism discussed above that the negative  $\omega_s$  shear is more effective than positive  $\omega_s$  shear in stabilizing the ITG mode under the weakly reversed magnetic shear. In comparison with the results with  $\omega_s = 0$  location at  $r/a = 0.20$ , when  $\omega_s = 0$  location at  $r/a = 0.25$  (the mode location), the linear growth rate does not decrease significantly, showing that stabilizing effect caused by  $E_r$  shear is noneffective.

Considering the weak effect of  $E_r$  for the condition that  $\omega_s = 0$  at  $r/a = 0.25$ , we made simulations for  $\omega_s^{max}/\gamma_0 = 0.0, 0.1, 0.2, 0.4, 0.6, 1.2$  in this case. The results are shown in Fig. 9b. The linear growth rates of the ITG mode with  $\omega_s^{max}/\gamma_0 = 0.1, 0.2$  are larger than  $\gamma_0$ , which are similar to the result under constant  $\omega_s$ . However, when the  $\omega_s^{max}/\gamma_0$  increases to 0.6, 1.2, the linear growth rate of the ITG mode not obviously decreases. The physics discussed in Section 3 can be used to explain the results in

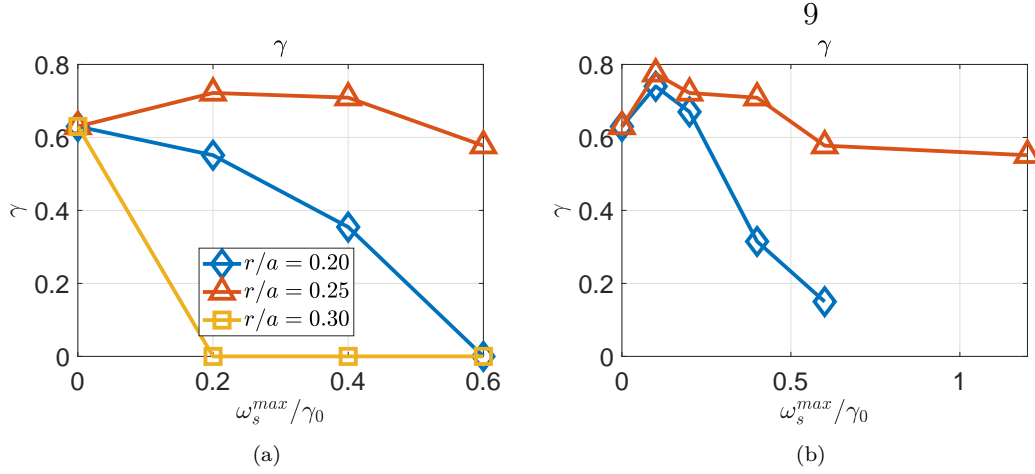


Figure 9: (a) The scanning results of setting  $\omega_s = 0$  at different radial location. Notice that the  $r/a = 0.20, 0.25, 0.30$  in legend means  $\omega_s = 0$  is located at  $r/a = 0.20, 0.25, 0.30$ . (b) The blue line represents the ITG growth rate versus  $\omega_s^{max}$  for  $E_r$  with different constant  $\omega_s$ . The red line denotes the ITG growth rate versus  $\omega_s^{max}$  for different amplitude of experimental  $E_r$  with  $\omega_s = 0$  at  $r/a = 0.25$ .

Fig. 9b. When  $E_r$  amplitude gets bigger, the  $\omega_s$  at the mode location  $r/a = 0.25$  is zero, but the  $\omega_s$  beside the  $r/a = 0.25$  gets bigger, which reduces the wavelength of the ITG mode [2]. The small wavelength causes the ITG mode to be locally limited near the  $r/a = 0.25$ , where has almost zero shearing rate, leading to weakly tilting effect of the ITG mode and no decreasing in the growth rate, which is shown in Fig. 10a–10c. The above results show that the local bottom of the  $E_r$  well is the most unfavorable region for stabilizing the ITG mode.

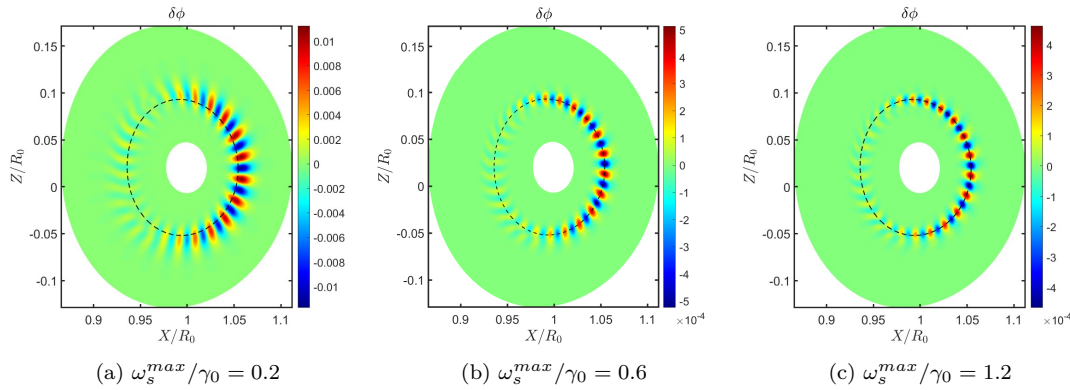


Figure 10: The poloidal mode structure of the real part of electrostatic potential with experimental  $E_r$  which  $\omega_s = 0$  at  $r/a = 0.25$ . The  $\omega_s^{max}/\gamma_0 = 0.2, 0.6, 1.2$ , respectively, and the dashed line indicates the largest  $\eta_i$  and  $q = 1$  positions.

Simulation results based on the experimental  $E_r$  profile show that the global effect of  $E_r$  should be considered even for the micro-instabilities such as ITG instability mode. The local bottom of  $E_r$  well has a negative impact on stabilizing the ITG instability mode. In the experiment, in the plasma core, the ion temperature and density increase with the formation of ITB [17], which means an increased ion pressure gradient. The

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 5 increasing ion pressure gradient raises the amplitude of the  $E_r$ , whose tilting effect  
 6 will become dominant compared with the weakly reverse magnetic shear and lead the  
 7 net effect stabilizes the ITG mode and reduces the turbulence transport. Besides, the  
 8 experiment research [18] showed that the  $E_r$  well bottom will shift outward in radial  
 9 direction, which matches our results that the  $E_r$  with  $\omega_s = 0$  location at  $r/a = 0.30$  has  
 10 more efficient stabilizing effect on ITG mode because of the synergistic effect between  
 11 the negative  $\omega_s$  and the weakly reverse magnetic shear. Therefore, it is very likely  
 12 that there is a mechanism of positive feedback between the formation of the ITB and  
 13 the formation of the  $E_r$ , leading to an increase in the  $E_r$  amplitude and the outward  
 14 movement of  $\omega_s$  location combined with the reversed magnetic shear, which might be the  
 15 key to the formation and the long-time existence of ITB. Moreover, in order to reduce  
 16 the transport by ITG, it is better to control the  $E_r$  with negative  $\omega_s$  in the reversed  
 17 magnetic shear region, e.g. using NBI which can induce plasma rotation to affect the  
 18  $E_r$  profile [19].  
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## 25 5. Conclusion

26  
 27 Based on EAST configuration, the synergistic effect of the  $E_r$  shear and magnetic  
 28 shear on turbulence is studied by GTC. In contrast to the previous stabilizing effect of  
 29 the  $E_r$  shear on ITG, it is found that whether the  $E_r$  shear is stabilizing or destabilizing  
 30 not only depends on the amplitude of the  $E_r$  shear, but also on the relative direction  
 31 between the  $E_r$  shear and the magnetic shear. Under the weakly reversed magnetic  
 32 shear,  $E_r$  shear is destabilizing for small positive shearing rate, while it is stabilizing  
 33 when positive shearing rate is large enough. For negative shearing rate,  $E_r$  shear always  
 34 plays a stable role, and is more efficient than that with positive shearing rate. Because  
 35 the negative  $\omega_s$  shear and the weakly magnetic shear have the same mode tilting  
 36 direction. The simulation results also indicate that the ITG mode is more unstable  
 37 under the positive magnetic shear.  
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42 The global effect of  $E_r$  profile should be considered in stabilizing ITG instability  
 43 for experimental  $E_r$ . The  $E_r$  with the  $\omega_s = 0$  at the right side of the ITG mode  
 44 shows a better stabilizing effect compared with the  $\omega_s = 0$  at the left side, because of  
 45 the synergistic effect of the negative  $\omega_s$  and the weakly reverse magnetic shear at the  
 46 ITG mode location. The positive feedback between the formation of the ITB and the  
 47 formation of the  $E_r$  will increase the  $E_r$  amplitude and cause the outward movement of  
 48 the  $\omega_s$  location combined with the reversed magnetic shear, which might be the key to  
 49 the formation and the long-time existence of ITB. Moreover, Neutral Beam Injection is  
 50 expected to manipulate the  $E_r$  profile with negative  $\omega_s$  in the reversed magnetic shear  
 51 region, which will stabilize ITG mode and reduce the transport by ITG mode. The  
 52 nonlinear simulations will be carried out in future, which might further illustrate the  
 53 synergistic effect on the ITG induced transport.  
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